Winning versus losing during gambling and its neural correlates

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Abstract-Humans often make decisions which maximize an internal utility function. For example, humans often maximize their expected reward when gambling and this is considered as a "rational" decision. However, humans tend to change their betting strategies depending on how they "feel". If someone has experienced a losing streak, they may "feel" that they are more likely to win on the next hand even though the odds of the game have not changed. That is, their decisions are driven by their emotional state. In this paper, we investigate how the human brain responds to wins and losses during gambling. Using a combination of local field potential recordings in human subjects performing a financial decision-making task, spectral analyses, and non-parametric cluster statistics, we investigated whether neural responses in different cognitive and limbic brain areas differ between wins and losses after decisions are made. In eleven subjects, the neural activity modulated significantly between win and loss trials in one brain region: the anterior insula (p = 0.01). In particular, gamma activity (30–70 Hz) increased in the anterior insula when subjects just realized that they won. Modulation of metabolic activity in the anterior insula has been observed previously in functional magnetic resonance imaging studies during decision making and when emotions are elicited. However, our study is able to characterize temporal dynamics of electrical activity in this brain region at the millisecond resolution while decisions are made and after outcomes are revealed.

I. INTRODUCTION

Decision-making links cognition to behavior and is a key driver of human personality, fundamental for survival, and essential for our ability to learn and adapt. It has been wellestablished that humans often make emotional-based decisions [1]. Thus, psychiatric patients who have dysfunctional cognitive circuitry, frequently have alterations in decisionmaking that are poorly understood.

Understanding the neural basis of decision-making is therefore essential toward patient management. However, access to the human brain has been limited to a few case studies wherein subjects have lesions in the key decision-making structures such as the orbital frontal cortex [2]–[4], or wherein functional magnetic resonance imaging (fMRI) is used to measure neural activity in several healthy subjects during decisionmaking [5]. Both of these approaches have limitations. Lesions don't provide actual neural data to ascertain a specific brain regions's role during behavior. Rather, the region's function is inferred by absence of behaviors from lesioned subjects when compared to healthy subjects. On the other hand, fMRI provides a correlate of neural activity (metabolic activity) but suffers from poor temporal resolution. fMRI resolution is on the order of multiple seconds, while decisions are often made on the order of tenths of a second.

Here, we took advantage of a technique called stereoelectroencephalography (SEEG) that allowed us to record high temporal resolution electrophysiological data (electrical activity at the millisecond scale) directly from deep and peripheral brain regions in human subjects while they performed a gambling task. These subjects are implanted with electrodes for clinical purposes, and each contact in the brain generates a local field potential (LFP) signal.

For our gambling task, eleven subjects played a game of high card where they won virtual money if their card was higher than the computer's card. On each trial, subjects had to decide to bet "high" (\$20) or "low" (\$5) on their card being higher than the hidden computer's card. Eighty percent of the trials lead to clear rational decisions where the expected reward for one choice is higher than another. On twenty percent of the trials, however, there is no clear rational decision since the expected reward is equal for both choices. Here, we focused on characterizing differences in brain activity between when a subject realizes that he/she has won versus when he/she has lost. Thus, the goal of this study is to assess the role of different brain regions in responding to outcomes of gambling decisions.

To identify neural correlates that encode a subject's response to a win versus a loss, we computed spectrograms for each brain region (i.e., electrode channel) and each patient across all trials when subjects won and compared them to spectrograms when subjects lost. Specifically, we examined spectral content before, during, and after the computer's card was shown (and hence outcome is revealed) and implemented a non-parametric cluster statistic to test whether the spectral activity differed between wins and losses in the given brain region. The nonparametric cluster test generates a cluster defined by a set of adjacent time-frequency windows that gives rise to the smallest p-value. If this p-value is smaller than 0.05, then the brain region (defined by location of the channel) was designated as encoding response to gambling outcome.

We found that upon examining several brain regions in cognitive, limbic and hippocampal networks, the anterior insula encoded information that separated wins from losses. Specifically, when gamma activity (30–70 Hz), was prevalent in this region, then the player was more likely to have won after he/she sees the computer's card. The anterior insula has been implicated in the role of emotions in risk-related decision

making [6] as well as being a neural basis for encoding how someone "feels" [7]. But no study has had access to electrical activity from these regions at a millisecond time-scale. Hence, these findings are the first to show evidence of temporal dynamics of rhythms in the brain at a fine resolution when decisions are made and when subjects "feel" the consequences of their decisions.

II. METHODS

A. Subjects

At the Cleveland Clinic, patients with medically intractable epilepsy routinely undergo SEEG recordings in order to localize the seizure focus. See II-B for details on the SEEG procedure. In this study, aside from the behavioral experiments, no alterations were made to the patient's clinical care, including the placement of the electrodes [8]. Subjects enrolled voluntarily and gave informed consent under criterion approved by the Cleveland Clinic Institutional Review Board. A total of eleven subjects volunteered to perform the task. Details on these recordings and eventual annotated seizure focus of these eleven patients are noted in Table I.

Subjects were implanted with 8 to 13 depth electrodes. Implantation was performed using robot-assisted surgery along with co-registered functional MRIs and angiograms to ensure safe implantation [9]. Once inserted, SEEG electrophysiological data were acquired using a Nihon Kohden 1200 EEG diagnostic and monitoring system (Nihon Kohden America, USA) at a sampling rate of 2 kHz. Behavioral event data were simultaneously acquired through the MonkeyLogic MATLAB[®] toolbox [10].

There are standard concerns in analyzing data from epileptic patients. First, patients are often on medication, which might affect the neurophysiology of the brain. For clinical purposes, patients were kept off of their anti-seizure medication for their entire stay at Cleveland Clinic, so these effects would be minimized. Secondly, actual seizures might impact the neurophysiology around the seizure focus. Human epilepsy recordings are taken to localize the seizure focus, so overlap is expected between seizure focus and areas recorded.

B. Stereoelectroencephalography

The Cleveland Clinic is a world-renowned center for the evaluation and treatment of epilepsy and brain tumors, assessing around 9500 patients every year from all 50 states and more than 10 countries. More than 400 epilepsy surgeries are performed every year, including a growing number of stereotactically implanted depth electrodes or stereoelectroencephalography (SEEG) [11]–[14]. This surgical procedure was developed in France [15]–[27], and brought to the United States by Dr. Jorge Gonzalez-Martinez [28]. The innovative approach using SEEG methodology relies on its capability in accessing large-scale networks, providing precise human brain data, from cortical to subcortical areas, in three-dimensional fashion. In routine placement of depth electrodes, burr-holes that are each 15 mm in diameter are required for safe visualization of cortical vessels, and therefore only a small

TABLE I

THIS TABLE PROVIDES CLINICALLY RELEVANT INFORMATION ON EACH SUBJECT: THE GENDER, THE AGE IN YEARS, AND THE DURATION OF EPILEPSY ("DUR.") IN YEARS. THIS TABLE ALSO PROVIDES THE NUMBER OF WIN, LOSS AND DRAW TRIALS.

ID	Gender	Age [yr.]	Dur. [yr.]	Win	Loss	Draw
1	male	26	3	73	73	39
2	female	41	38	79	58	25
3	female	55	52	23	34	15
4	female	31	13	53	57	34
5	female	53	23	50	61	25
6	female	60	8	63	88	21
7	female	36	36	56	68	33
8	female	23	5	46	50	36
9	male	32	11	65	59	36
10	female	32	13	57	62	35
11	male	28	11	67	78	37

number of electrodes are placed. SEEG placement, however, uses several small drill holes (1.8 mm in diameter), allowing many electrodes to be inserted.

Since direct visualization of the cortical surface is not possible with small drills (Fig. 1A), the SEEG technique requires detailed pre-procedural vascular mapping using pre-operative imaging with magnetic resonance angiography (MRA) and cerebral angiography. Angiography is an X-ray examination of the blood vessels. The mapping procedure is performed under fluoroscopy using general anesthesia, and an expert neuro-anesthesiologist correctly titrates anesthesia to permit measurement of intracranial electroencephalography (EEG). The number and location of implanted electrodes are preoperatively planned based on a pre-implantation hypothesis, which is formulated in accordance with non-invasive preimplantation data, such as seizure semiology, ictal and interictal scalp EEG, magnetic resonance imaging (MRI), positron emission tomography (PET) and ictal single-photon emission computed tomography (SPECT) scans. Thus, the implantation strategy has the goal of accepting or rejecting the preimplantation hypothesis of the location of the epileptogenic zone (EZ).

SEEG provides a more complete coverage of the brain, from lateral, intermediate and/or deep structures in a threedimensional arrangement recorded over hundreds of channels. Using strict techniques, this procedure is safe and minimally invasive: only 1/1176 implantations last year resulted in an asymptomatic intracranial hemorrhage. The rate of complications in SEEG implantations is less than 1 % [13], [29].

C. Gambling task

Subjects performed the gambling task in their Epilepsy Monitoring Unit room. The task was displayed via a computer screen and the subject interacted with the task using an InMotion2 robotic manipulandum (Interactive Motion Technologies,

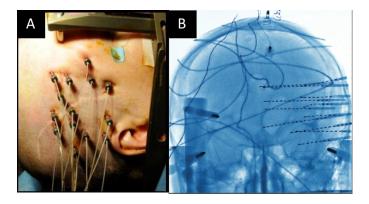


Fig. 1. Imaging fusion and placement of multiple electrodes using the SEEG method. Fig. A is a photograph showing 14 electrodes at the skin surface. Fig. B is a fluoroscopy image of an SEEG-implanted subject (coronal view with eye forward). Note the precise parallel placement, with tips terminating at the midline or dural surface.

USA). The manipulandum is controlled by the subject's hand and allows for 2D planar motion, which translated directly to the position of a cursor on screen.

The gambling task (Fig. 2A) is based on a simple game of high card where subjects would win virtual money if their card beat the computer's card. Specifically, in the beginning of each trial, the subject controlled a cursor via a planar manipulandum to a fixation target. Afterwards, the subject is shown his card (2, 4, 6, 8, or 10) that is randomly chosen with equal distribution. The computer's card is initially hidden. The screen then shows their two choices: a high bet (\$20) or a low bet (\$5). The subject has 6 seconds to select one with his cursor. Following selection, the computer's card, which follows the same distribution, is revealed. The final screen depicts the amount won or lost.

D. Data analysis

All electrophysiological and behavioral analyses were conducted offline using custom MATLAB[®] scripts.

Data for 16 anatomical regions in cognitive, limbic and hippocampal networks were separated into win and loss trials. For each brain region, differences in the neural responses between the task conditions during the 250 ms before and 1000 ms after the computer card were examined by means of a nonparametric cluster statistic. Specifically, spectrograms were constructed for each trial time-locked to when the computer's card is shown. Then the spectrograms for win trials were compared to those for loss trials. To see if spectrograms for each group were statistically significantly different, we used a nonparametric cluster-based test [30]. Clusters are defined as a set of adjacent time-frequency windows whose activity is statistically significant between trials where the subject ends up winning versus losing.

1) Spectral analysis: We calculated the oscillatory power using multitapers from the Chronux toolbox [31]. We used three orthogonal tapers with a 300 ms window sliding at 50 ms steps. We dropped frequencies under 10 Hz because of the Nyquist criterion and analyzed upwards to 100 Hz. Afterwards,

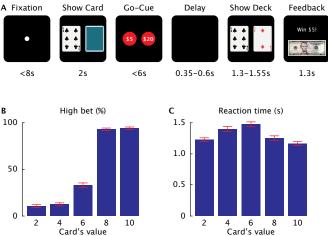


Fig. 2. Gambling task and behavioral results. (A) Timeline of the behavioral task. After fixation, subjects were shown their card. Once the bets were shown, subjects selected one of the choices and then were shown the computer's card following a delay. Feedback was provided afterwards by displaying the amount won or lost. (B) Average bet decisions across cards. Subjects predominantly bet low for 2 and 4 cards and bet high for 8 and 10 cards. There was no predominant strategy for 6 cards, which had bout 33 % chance of eliciting a high bet. (C) Reaction times across cards. Subjects reacted faster for cards whose rewards had lower variability.

we normalize each frequency bin's power by first taking the natural log of the power in each frequency bin, and then performing a Gaussian normalization based on the power in each frequency bin over the entire recording session.

2) Non-parametric cluster statistical test: Significant differences between the neural response data in each anatomical region are defined by a non-parametric cluster statistic run on data aggregated from trials by all relevant subjects [30].

This test leverages the dependency between adjacent timefrequency windows in order to avoid over-penalizing with multiple comparison corrections. For each time-frequency window in the spectrogram, a null distribution was created by shuffling these wins and loss labels 1000 times between trials within each subject. Within each shuffle, the average difference between the newly labeled win and loss trial spectrograms was calculated. A p-value was assigned for each window by comparing the difference acquired from the true labels with the distribution of differences acquired from the shuffled labels. Clusters were formed by grouping windows with significant p-values (p < 0.05) that were adjacent in either time or frequency. The test statistic for each cluster was calculated by taking the sum of the log of the *p*-values for each window in the cluster. This prioritizes clusters that both have strong differences as well as large sizes. A null distribution of cluster statistics was created using the same process but with the 1000 spectrograms obtained from the originally shuffled labels. The observed cluster statistic was then compared against this null distribution of cluster statistics in order to obtain the final *p*-value of the test.

Brain region	Subj.	Win	Loss	<i>p</i> -value
parieto-occipital sulcus	7	397	433	-
inferior frontal gyrus	6	362	384	-
middle frontal gyrus	5	270	308	
inferior temporal gyrus	10	576	620	
hippocampus	10	576	620	
hippocampus (posterior)	4	225	226	
intraparietal sulcus	6	374	399	
anterior cingulate	3	173	207	
cuneus	10	582	627	-
angular gyrus	8	444	495	
orbitofrontal cortex	4	249	254	
amygdala	2	124	140	
posterior cingulate	9	552	592	
precuneus	9	517	568	
insula	7	423	420	•
anterior insula	2	103	118	
				0 † 1 0.05

Fig. 3. Non-parametric cluster statistic for different brain regions. For each brain region, differences in the neural responses between the task conditions during the 250 ms before and 1000 ms after the show computer card epoch were summarized by means of a non-parametric cluster statistic (*p*-value). In addition, we provide the number of subjects with recording in this area (Subj.), and the number of win and loss trials.

III. RESULTS

This section summarizes the main findings of our analysis. First, we show the *p*-value associated with 16 brain regions. Then, we focus on the brain region identified in our exploratory analysis and show time-frequency differences of the neural responses around the show computer card epoch.

While multiple brain regions appear to show some response (data not shown), the two task conditions only significantly differ after the computer card is shown in one brain region: anterior insula (p = 0.01) (see Fig. 3). All *p*-values are computed from a non-parametric cluster statistic described in Section II.

Differences in the neural responses around the show computer card epoch was examined for the anterior insula (Fig. 4). Spectrograms of the neural responses between win and loss conditions show large differences in the gamma band (30– 70 Hz) after the computer card is shown and the gambling outcome is revealed.

We summarize the neural activity in the time-frequency domain by averaging the responses over 70–100 Hz. Gamma activity increases in anterior insula quickly around 250 ms after the computer card epoch and then decreases slowly until 1000 ms after the computer card epoch (Fig. 5). The gamma activity for win trials decreases more slowly than gamma activity for loss trials.

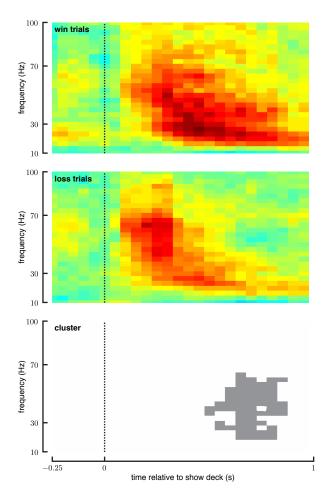


Fig. 4. Differences in the neural responses during the 250 ms before and 1000 ms after the show computer card epoch for anterior insula. (First and second rows) Spectrograms of the neural responses show differences in the time-frequency domain between win and loss conditions. (Third row) The cluster emphasizes the region of the time-frequency domain where the neural responses show significant differences between win and loss conditions (p < 0.05).

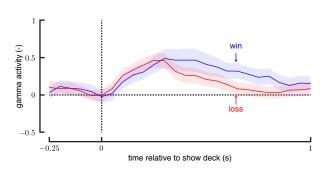


Fig. 5. Gamma activity (30–70 Hz) increases in anterior insula quickly around 250 ms after the computer card epoch and then decreases slowly until 1000 ms after the computer card epoch. The gamma activity for win trials decreases more slowly than gamma activity for loss trials.

IV. CONCLUSION

In our subject population, the neural activity modulated significantly between win and loss trials in the anterior insula (p = 0.01). In particular, gamma-band activity increased around 500 ms after the show computer card for win trials. The anterior insula has been implicated in the role of emotions in risk-related decision making [6] as well as being a neural basis for encoding how someone "feels" [7], but no study has had access to electrical activity from these regions at a millisecond time-scale. Hence, these findings are the first to show evidence of temporal dynamics of rhythms in the brain at a fine resolution when decisions are made and when subjects "feel" the consequences of their decisions. Still, the exact mechanisms by which this region in involved in risk-based decision making are not known and will therefore remain the focus of future work.

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REFERENCES

- [1] M. Toda, "Emotion and decision making," *Acta Psychologica*, vol. 45, no. 1–3, pp. 133–155, 1980.
- [2] A. Bechara, "The role of emotion in decision-making: Evidence from neurological patients with orbitofrontal damage," *Brain and Cognition*, vol. 55, no. 1, pp. 30 – 40, 2004. Development of Orbitofrontal Function.
- [3] J. Kim and M. E. Ragozzino, "The involvement of the orbitofrontal cortex in learning under changing task contingencies," *Neurobiology of Learning and Memory*, vol. 83, no. 2, pp. 125 – 133, 2005.
- [4] I. Bohn, C. Giertler, and W. Hauber, "Orbital prefrontal cortex and guidance of instrumental behaviour in rats under reversal conditions," *Behavioural Brain Research*, vol. 143, no. 1, pp. 49 – 56, 2003.
- [5] N. K. Logothetis, "What we can do and what we cannot do with fmri," *Nature*, vol. 453, pp. 869–878, 06 2008.
- [6] A. G. Sanfey, J. K. Rilling, J. A. Aronson, L. E. Nystrom, and J. D. Cohen, "The neural basis of economic decision-making in the ultimatum game," *Science*, vol. 300, no. 5626, pp. 1755–1758, 2003.
- [7] A. D. B. Craig, "How do you feel—now? the anterior insula and human awareness," *Nat Rev Neurosci*, vol. 10, pp. 59–70, Jan. 2009.
- [8] M. A. Johnson, S. Thompson, J. Gonzalez-Martinez, H.-J. Park, J. Bulacio, I. Najm, K. Kahn, M. Kerr, S. V. Sarma, and J. T. Gale, "Performing behavioral tasks in subjects with intracranial electrodes," *Journal of Visualized Experiments*, no. 92, p. e51947, 2014.
- [9] D. Öngür and J. Price, "The organization of networks within the orbital and medial prefrontal cortex of rats, monkeys and humans," *Cerebral Cortex*, vol. 10, no. 3, pp. 206–219, 2000.
- [10] W. F. Asaad and E. N. Eskandar, "A flexible software tool for temporallyprecise behavioral control in matlab," *Journal of Neuroscience Methods*, vol. 174, no. 2, pp. 245 – 258, 2008.
- [11] J. Gonzalez-Martinez and D. Lachhwani, "Stereoelectroencephalography in children with cortical dysplasia: technique and results," *Child's Nervous System*, vol. 30, no. 11, pp. 1853–1857, 2014.
- [12] J. Gonzalez-Martinez, J. Mullin, J. Bulacio, A. Gupta, R. Enatsu, I. Najm, W. Bingaman, E. Wyllie, and D. Lachhwani, "Stereoelectroencephalography in children and adolescents with difficult-to-localize refractory focal epilepsy," *Neurosurgery*, vol. 75, no. 3, pp. 258–268, 2014.
- [13] J. Gonzalez-Martinez, J. Mullin, S. Vadera, J. Bulacio, G. Hughes, S. Jones, R. Enatsu, and I. Najm, "Stereotactic placement of depth electrodes in medically intractable epilepsy," *Journal of Neurosurgery*, vol. 120, no. 3, pp. 639–644, 2014.

- [14] J. Gonzalez-Martinez and I. M. Najm, "Indications and selection criteria for invasive monitoring in children with cortical dysplasia," *Child's Nervous System*, vol. 30, no. 11, pp. 1823–1829, 2014.
- [15] J. Bancaud, J. Talairach, S. Geier, A. Bonis, S. Trottier, and M. Manrique, "[Behavioral manifestations induced by electric stimulation of the anterior cingulate gyrus in man]," *Rev Neurol*, vol. 132, pp. 705–724, Oct. 1976.
- [16] J. Bancaud, J. Talairach, M. Lamarche, A. Bonis, and S. Trottier, "[Neurophysiopathological hypothesis on startle epilepsy in man]," *Rev Neurol*, vol. 131, pp. 559–571, Aug. 1975.
- [17] J. Bancaud, J. Talairach, P. Morel, and M. Bresson, "[Ammon's horn and amygdaline nucleus: clinical and electric effects of their stimulation in man]," *Revue neurologique*, vol. 115, pp. 329–352, Sept. 1966.
- [18] J. Bancaud, J. Talairach, P. Morel, M. Bresson, A. Bonis, S. Geier, E. Hemon, and P. Buser, ""Generalized" epileptic seizures elicited by electrical stimulation of the frontal lobe in man," *Electroencephalogr Clin Neurophysiol*, vol. 37, pp. 275–282, Sept. 1974.
- [19] J. Bancaud, J. Talairach, P. Waltregny, M. Bresson, and P. Morel, "[Stimulation of focal cortical epilepsies by megimide in topographic diagnosis (clinical EEG and SEEG study)]," *Revue neurologique*, vol. 119, pp. 320–325, Sept. 1968.
- [20] J. Bancaud, J. Talairach, P. Waltregny, M. Bresson, and P. Morel, "Activation by Megimide in the topographic diagnosis of focal cortical epilepsies (clinical EEG and SEEG study)," *Electroencephalography and clinical neurophysiology*, vol. 26, p. 640, June 1969.
- [21] J. Talairach and G. Szikla, "[Amygdalo-hippocampal partial destruction by yttrium-90 in the treatment of certain epilepsies of rhinencephalic manifestation]," *Neurochirurgie*, vol. 11, no. 3, pp. 233–240, 1965.
- [22] J. Talairach and G. Szikla, "Application of stereotactic concepts to the surgery of epilepsy," in Advances in Stereotactic and Functional Neurosurgery 4 (F. Gillingham, J. Gybels, E. Hitchcock, G. Rossi, and G. Szikla, eds.), vol. 30 of Acta Neurochirurgica Supplementum, pp. 35– 54, Springer Vienna, 1980.
- [23] J. Talairach, P. Tournoux, A. Musolino, and O. Missir, "Stereotaxic exploration in frontal epilepsy," *Advances in neurology*, vol. 57, pp. 651– 688, 1992.
- [24] J. Bancaud, J. Talairach, A. Bonis, C. Schaub, G. Szikla, P. Morel, and M. Bordas-Ferer, La stéréo-électroencéphalographie dans l'épilepsie. Informations neurophysiopathologiques apportées par l'investigation fonctionnelle stéréotaxique. Masson, 1965.
- [25] C. Munari, J. Bancaud, A. Bonis, P. Buser, J. Talairach, and G. Szikla, "[Role of the amygdala in the occurence of oro-alimentary signs of during epileptic seizures in man]," *Revue d'électroencéphalographie et de neurophysiologie clinique*, vol. 9, no. 3, pp. 236–240, 1979.
- [26] C. Munari, L. Bossi, C. Stoffels, P. Brunet, J. Bancaud, J. Talairach, and P. L. Morselli, "[Cerebral concentrations of anticonvulsants in patients with epilepsy of tumoral origin]," *Revue d'électroencéphalographie et de neurophysiologie clinique*, vol. 12, pp. 38–43, Apr 1982.
- [27] C. Munari, A. Giallonardo, P. Brunet, D. Broglin, and J. Bancaud, "Stereotactic investigations in frontal lobe epilepsies," in *Advances in Stereotactic and Functional Neurosurgery* 8 (G. Broggi, J. Burzaco, E. Hitchcock, B. Meyerson, and S. Tóth, eds.), vol. 46 of *Acta Neurochirurgica Supplementum*, pp. 9–12, Springer Vienna, 1989.
- [28] J. Gonzalez-Martinez, J. Bulacio, A. Alexopoulos, L. Jehi, W. Bingaman, and I. Najm, "Stereoelectroencephalography in the "difficult to localize" refractory focal epilepsy: Early experience from a north american epilepsy center," *Epilepsia*, vol. 54, no. 2, pp. 323–330, 2013.
- [29] F. Cardinale and G. Lo Russo, "Stereo-electroencephalography safety and effectiveness: Some more reasons in favor of epilepsy surgery," *Epilepsia*, vol. 54, no. 8, pp. 1505–1506, 2013.
- [30] E. Maris and R. Oostenveld, "Nonparametric statistical testing of EEGand MEG-data," *Journal of Neuroscience Methods*, vol. 164, no. 1, pp. 177–190, 2007.
- [31] H. Bokil, P. Andrews, J. E. Kulkarni, S. Mehta, and P. P. Mitra, "Chronux: A platform for analyzing neural signals," *Journal of Neuroscience Methods*, vol. 192, no. 1, pp. 146–151, 2010.