## Knowledge representation (INFO0049-1) Exercise session 2

24 Feb 2015

\*\*\*Try to draw search trees wherever possible to see how prolog executes a query\*\*\*

## Arithmetic Exercise

1. Write a predicate sum(+Number, -Sum) that succeeds if 'Sum' is the sum of all the digits in the positive integer number 'Number'.

?- sum(26, X).

X = 8; true.

2. Define a predicate is\_even(+Number) that succeeds if the positive integer number 'Number' is an even number and fails otherwise.

?- is\_even(36789).

true.

Extend the above and write another predicate all\_even(+Number) that succeeds if all the digits in the number 'Number' are even. Draw search trees for all\_even(36789) and all\_even(688).

?- all\_even(468).

true.

?- all\_even(4638).

false.

3. Write a predicate is\_double(+Number) that succeeds if the positive integer number 'Number' contains two equal digits. For example, is\_double(12452) succeeds whereas is\_double(134567) fails.

?- is\_double(134567)

false.

?- is\_double(12452)

true.

4. Define a predicate gcd(+A, +B, -C) that succeeds if C is the GCD (greatest common divisor) of the two positive integer numbers A and B.

?- gcd(2,6,X).

X = 2; false.

5. Define a predicate prime(+Number) that succeeds if 'Number' is a prime number.

?- prime(3)

true.

6. Goldbach's conjecture is one of the most famous facts in number theory that has not been proved to be correct in the general case. It says that: Every positive even number greater than 2 is the sum of two prime numbers.

Example: 28 = 5 + 23.

Define a predicate goldbach(+X, -Y, -Z) that succeeds if X = Y + Z where X is an even integer greater than 2 and Y, Z two prime numbers.